

Discussion 1

6/23

What did we cover?

- * How do we **control** what code is executed?
- * How **many times** is it executed?
- * How do we **access** elements in a list?
- * How do we **visualize** code?

What did we cover?

- * How do we **control** what code is executed? **If statements**
- * How **many times** is it executed? **While loops**
- * How do we **access** elements in a list? **lst[0]**
lst[1:3]
- * How do we **visualize** code? **environment diagrams!**

Control Structures

If Statements

- * Only execute the code that corresponds to the first true conditional
- * If none of the conditionals are true, execute the else (if it exists)

What Would Python Do?

```
if True:
    print("hi")
elif True:
    print("61A")
else:
    print("rocks!")
```



```
if True:
    print("hi")
if True:
    print("61A")
else:
    print("rocks!")
```



hint: how does a sequence of if conditions behave differently from a sequence of elif's after an if?

What Would Python Do?

```
if True:
    print("hi")
elif True:
    print("61A")
else:
    print("rocks!")
```

hi

```
if True:
    print("hi")
if True:
    print("61A")
else:
    print("rocks!")
```

hi
61A

What Would Python Do?

```
if True:
    return "hi"
elif True:
    return "61A"
else:
    return "rocks!"
```



```
if True:
    return "hi"
    if True:
        return "61"
else:
    return "rocks!"
```



hint: how does `return` behave differently from `print`?

What Would Python Do?

```
if True:  
    return "hi"  
elif True:  
    return "61A"  
else:  
    return "rocks!"
```

'hi'

```
if True:  
    return "hi"  
if True:  
    return "61"  
else:  
    return "rocks!"
```

'hi'

1.3 #2

```
def handle_overflow(s1, s2):  
    """  
  
    >>> handle_overflow(27, 15)  
  
    No overflow  
  
    >>> handle_overflow(35, 29)  
  
    1 spot left in Section 2  
  
    >>> handle_overflow(20, 32)  
  
    10 spots left in Section 1  
  
    >>> handle_overflow(35, 30)  
  
    No space left in either section  
  
    """
```


1.3 #2

What conditions do we have?

```
def handle_overflow(s1, s2):
```

```
    """
```

```
>>> handle_overflow(27, 15)
```

```
No overflow
```

```
>>> handle_overflow(35, 29)
```

```
1 spot left in Section 2
```

```
>>> handle_overflow(20, 32)
```

```
10 spots left in Section 1
```

```
>>> handle_overflow(35, 30)
```

```
No space left in either section
```

```
    """
```

hint: use doctests to figure out how the different arguments affect what the function does

1.3 #2

What conditions do we have?

```
def handle_overflow(s1, s2):
```

Look at the doctests to determine what conditions produce different results

```
"""
```

```
>>> handle_overflow(27, 15)
```

Both numbers under 30

```
No overflow
```

```
>>> handle_overflow(35, 29)
```

First number (s1) larger than 30

```
1 spot left in Section 2
```

```
>>> handle_overflow(20, 32)
```

Second number (s2) larger than 30

```
10 spots left in Section 1
```

```
>>> handle_overflow(35, 30)
```

Both numbers larger than OR EQUAL TO 30

```
No space left in either section
```

```
"""
```

hint: use doctests to figure out how the different arguments affect what the function does

doctest

1.3 #2

What do we do for each condition?

(don't worry about "spot" vs. "spots" yet)

```
def handle_overflow(s1, s2):
```

```
    """
```

```
>>> handle_overflow(27, 15)
```

```
No overflow
```

```
>>> handle_overflow(35, 29)
```

```
1 spot left in Section 2
```

```
>>> handle_overflow(20, 32)
```

```
10 spots left in Section 1
```

```
>>> handle_overflow(35, 30)
```

```
No space left in either section
```

```
    """
```

hint: use doctests to figure out what the different actions of the function should be

doctest

1.3 #2

What do we do for each condition?

(don't worry about "spot" vs. "spots" yet)

Both numbers under 30

—> Print "No overflow"

First number (s1) larger than 30

—> Print "x spots left in Section s2"

Second number (s2) larger than 30

—> Print "x spots left in Section s1"

Both numbers larger than OR
EQUAL TO 30

—> Print "No space left in either section"

```
def handle_overflow(s1, s2):
```

```
    """
```

```
>>> handle_overflow(27, 15)
```

```
No overflow
```

```
>>> handle_overflow(35, 29)
```

```
1 spot left in Section 2
```

```
>>> handle_overflow(20, 32)
```

```
10 spots left in Section 1
```

```
>>> handle_overflow(35, 30)
```

```
No space left in either section
```

```
    """
```

hint: use doctests to figure out what the different actions of the function should be

doctest

1.3 #2

Putting the results of the previous slide into code, we get:

```
def handle_overflow(s1, s2):  
    if s1 < 30 and s2 < 30:  
        print("No overflow")  
    elif s1 < 30:  
        print(30 - s1, "spots left in Section 2")  
    elif s2 < 30:  
        print(30 - s2, "spots left in Section 1")  
    else:  
        print("No space left in either section")
```


1.3 #2

Now let's worry about "spot" vs. "spots"

Where in the code should we differentiate between printing "spot" and "spots"?

```
def handle_overflow(s1, s2):  
    if s1 < 30 and s2 < 30:  
        print("No overflow")  
    elif s1 < 30:  
        print(30 - s1, "spots left in Section 2")  
    elif s2 < 30:  
        print(30 - s2, "spots left in Section 1")  
    else:  
        print("No space left in either section")
```


1.3 #2

Now let's worry about "spot" vs. "spots"

Where in the code should we differentiate between printing "spot" and "spots"?

```
def handle_overflow(s1, s2):  
    if s1 < 30 and s2 < 30:  
        print("No overflow")  
    elif s1 < 30:  
        print(30 - s1, "spots left in Section 2")  
    elif s2 < 30:  
        print(30 - s2, "spots left in Section 1")  
    else:  
        print("No space left in either section")
```

So if there is only 1 spot left, we should print "spot" Otherwise we print "spots"

1.3 #2

```
def handle_overflow(s1, s2):  
    if s1 < 30 and s2 < 30:  
        print("No overflow")  
    elif s1 < 30:  
        if 30 - s1 == 1:  
            print(30 - s1, "spot left in Section 2")  
        else:  
            print(30 - s1, "spots left in Section 2")  
    elif s2 < 30:  
        if 30 - s2 == 1:  
            print(30 - s1, "spot left in Section 1")  
        else:  
            print(30 - s1, "spots left in Section 1")  
    else:  
        print("No space left in either section")
```


1.5 #2

Fill in the `is_prime` function, which returns `True` if `n` is a prime number and `False` otherwise.

Hint: use the `%` operator

```
def is_prime(n):
```

1.5 #2

Fill in the `is_prime` function, which returns `True` if `n` is a prime number and `False` otherwise.

Hint: use the `%` operator

~~`def is_prime(n):`~~

Wait! Before you even think about writing code, write down what you know!

1.5 #2

Fill in the `is_prime` function, which returns `True` if `n` is a prime number and `False` otherwise.

Hint: use the `%` operator

~~`def is_prime(n):`~~

Wait! Before you start writing code, write down what you know!

- * What are the arguments?
- * What do we want to return?
- * What kind of programming constructs that we learned can you use to solve this problem?

hint: before writing code, make sure you understood the problem

1.5 #2

We want to determine **whether or not n is prime**. A number is prime if its only divisors are 1 and itself.

So if dividing n by any number smaller than it produces a **non zero remainder**, then n is definitely prime.

How can we check that all numbers smaller than n will produce a non zero remainder?

How do we return **False** if we get 0 as a remainder somewhere?

How do we return **True** otherwise?

hint: if you can answer all of these questions, you are basically done with the problem

1.5 #2

Formalizing the answers the questions from the previous slide:

```
def is_prime(n):  
    if n == 1:  
        return False  
    k = 2  
    while k < n:  
        if n % k == 0:  
            return True  
        k += 1  
    return True
```


1.5 #2

Check yourself:

Why do we need the first if statement? What will happen if we start the while loop with $k = 1$?

Why is it ok for us to just return True after the while loop? In other words: can we ever return True on accident when n is actually prime?

1.6 #1

Implement `fizzbuzz(n)` which prints the numbers from 1 to `n` inclusive. For numbers divisible by 3, print “fizz”. For numbers divisible by 5 print “buzz”. For numbers divisible by both print “fizzbuzz”.

```
def fizzbuzz(n):
```


1.6 #1

Implement `fizzbuzz(n)` which prints the numbers from 1 to `n` inclusive. For numbers divisible by 3, print “fizz”. For numbers divisible by 5 print “buzz”. For numbers divisible by both print “fizzbuzz”.

~~`def fizzbuzz(n):`~~

Wait! Before you start writing code, write down what you know!

- * What are the arguments?
- * What do we want to return?
- * What kind of programming constructs that we learned can you use to solve this problem?

1.6 #1

```
def fizzbuzz(n):
```

```
    i = 1  
    while i <= n:
```

We need to print something for each number from 1 to n
So we should have a **while** loop!

1.6 #1

```
def fizzbuzz(n):
```

```
    i = 1
```

```
    while i <= n:
```

```
        if i % 3 == 0 and i % 5 == 0:
```

```
            print('fizzbuzz')
```

```
        elif i % 3 == 0:
```

```
            print('fizz')
```

```
        elif i % 5 == 0:
```

```
            print('buzz')
```

```
        else:
```

We need to print something for each number from 1 to n
So we should have a **while** loop!

Use the modulus operator to check if a number is divisible by 3, 5, or both.

Why does the order of the if statements matter here?

1.6 #1

```
def fizzbuzz(n):
```

```
    i = 1  
    while i <= n:
```

We need to print something for each number from 1 to n
So we should have a while loop!

```
        if i % 3 == 0 and i % 5 == 0:
```

```
            print('fizzbuzz')
```

```
        elif i % 3 == 0:
```

```
            print('fizz')
```

```
        elif i % 5 == 0:
```

```
            print('buzz')
```

```
        else:
```

```
            print(i)
```

Use the modulus operator to check if a number is divisible by 3, 5, or both.

Why does the order of the if statements matter here?

If none of the conditions are met, just print out the number

1.6 #1

```
def fizzbuzz(n):
```

```
    i = 1  
    while i <= n:
```

We need to print something for each number from 1 to n
So we should have a **while** loop!

```
        if i % 3 == 0 and i % 5 == 0:
```

```
            print('fizzbuzz')
```

```
        elif i % 3 == 0:
```

```
            print('fizz')
```

```
        elif i % 5 == 0:
```

```
            print('buzz')
```

```
        else:
```

```
            print(i)
```

```
        i += 1
```

Don't forget to increment i each time!

Use the modulus operator to check if a number is divisible by 3, 5, or both.

Why does the order of the if statements matter here?

If none of the conditions are met, just print out the number

Lists and For Statements

2.1 Example

```
>>> pizza = [1, 2, 3, 4]
```

```
>>> pizza[1:2]
```

2.1 Example

```
>>> pizza = [1, 2, 3, 4]
```

```
>>> pizza[1:2] ← Think of this as getting the elements of  
pizza that are from index 1 to index 2,  
not including index 2 — [1, 2)
```

```
[2]
```

Note: this returns the list [2], not just
the number 2

2.1 Example

```
>>> pizza = [1, 2, 3, 4]
```

```
>>> pizza[1:2] ← Think of this as getting the elements of  
pizza that are from index 1 to index 2,  
not including index 2 — [1, 2)
```

```
[2]
```

Note: this returns the list [2], not just
the number 2

```
>>> pizza[1:]
```

2.1 Example

```
>>> pizza = [1, 2, 3, 4]
```

```
>>> pizza[1:2] ← Think of this as getting the elements of  
pizza that are from index 1 to index 2,  
not including index 2 — [1, 2)
```

```
[2]
```

Note: this returns the list [2], not just
the number 2

```
>>> pizza[1:]=] Not specifying the last index means “till  
the end of the list”  
[2, 3, 4]
```


2.1 Example

```
>>> pizza = [1, 2, 3, 4]
```

```
>>> pizza[1:2] ← Think of this as getting the elements of  
pizza that are from index 1 to index 2,  
not including index 2 — [1, 2)
```

```
[2]
```

Note: this returns the list [2], not just
the number 2

```
>>> pizza[1:]= Not specifying the last index means “till  
the end of the list”
```

```
[2, 3, 4]
```

```
>>> pizza[-2:3]
```


2.1 Example

```
>>> pizza = [1, 2, 3, 4]
```

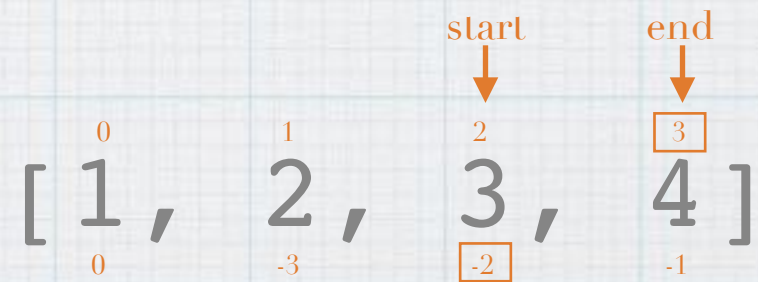
```
>>> pizza[1:2] ← Think of this as getting the elements of  
pizza that are from index 1 to index 2,  
not including index 2 — [1, 2)
```

```
[2]
```

Note: this returns the list [2], not just
the number 2

```
>>> pizza[1:]= Not specifying the last index means “till  
the end of the list”  
[2, 3, 4]
```

```
>>> pizza[-2:3]  
[3]
```



Find the start and end indices and
return everything between them except
for the last element

Environment Diagrams

There are 3 types of things you
should be able to draw out

There are 3 types of things you should be able to draw out

bob = 3

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

I like to keep track of the current frame → CF: G
up here


Global Frame:

There are 3 types of things you should be able to draw out

bob = 3

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

I like to keep track of the current frame  CF: G
up here

Global Frame:

bob: 3

There are 3 types of things you should be able to draw out

```
bob = 3
```


ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

```
def rob(bob):  
    a = 2  
    return 'mob'
```

DEF STATEMENTS

1. Write the function name in the current frame
2. Point it to the function object which we represent by the function signature and parent

I like to keep track of the **current frame**  **CF: G**
up here

Global Frame:
bob: 3

There are 3 types of things you should be able to draw out

bob = 3

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

```
def rob(bob):  
    a = 2  
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DEF STATEMENTS

1. Write the function name in the current frame
2. Point it to the function object which we represent by the function signature and parent

I like to keep track of the **current frame** up here → CF: G

Global Frame:

bob: 3

rob: → func rob(bob) [P=G]

Where is this function being defined? What is your current frame?



There are 3 types of things you should be able to draw out

bob = 3

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

```
def rob(bob):  
    a = 2  
    return 'mob'
```

DEF STATEMENTS

1. Write the function name in the current frame
2. Point it to the function object which we represent by the function signature and parent

bob = rob **What will this ASSIGNMENT do?**

I like to keep track of the **current frame** up here → CF: G

Global Frame:

bob: 3

rob: → func **rob**(bob) [P=G]

Where is this function being defined? What is your current frame?



There are 3 types of things you should be able to draw out

bob = 3

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

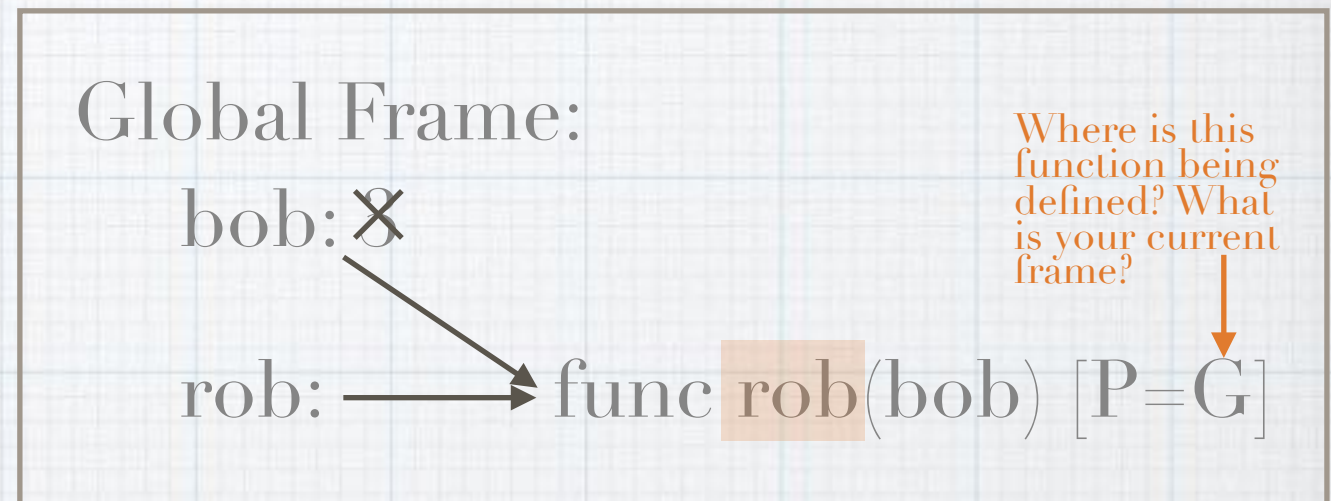
```
def rob(bob):  
    a = 2  
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DEF STATEMENTS

1. Write the function name in the current frame
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bob = rob **What will this ASSIGNMENT do?**

I like to keep track of the **current frame** up here → CF: G



There are 3 types of things you should be able to draw out

`bob = 3`

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

`def rob(bob):`
 `a = 2`
 `return 'mob'`

DEF STATEMENTS

1. Write the function name in the current frame
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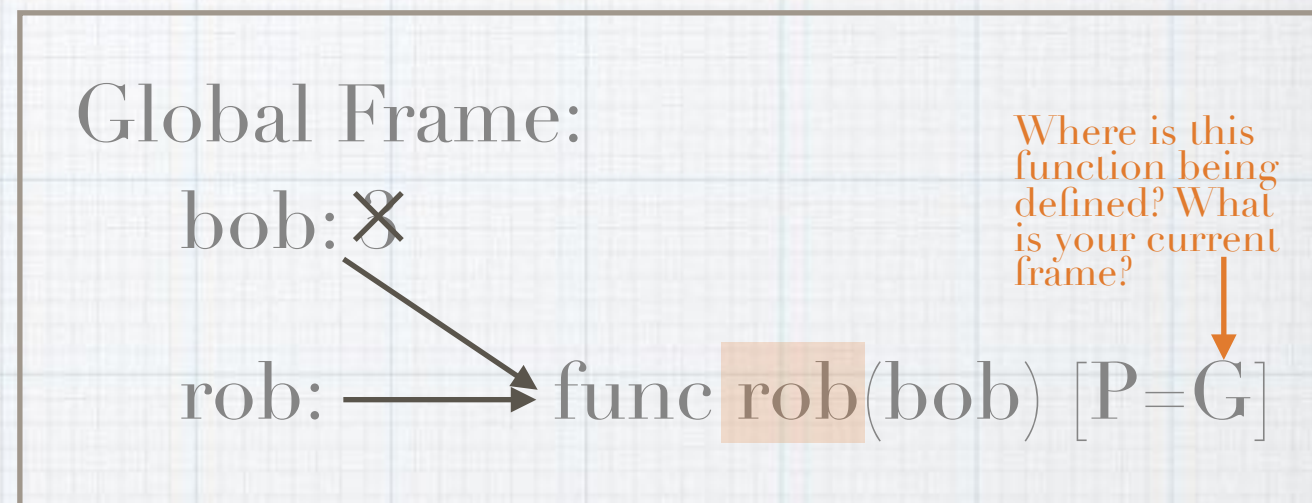
`bob = rob` What will this **ASSIGNMENT** do?

`bob = bob(bob)` bob points to the function rob in the global frame, so we call the rob function

FUNCTION CALLS

1. Evaluate the operator and operand
2. Open a new frame
Write f#: function name [P = ???]
(optional; update your current frame in CF:)
Assign the parameters
3. Execute the body of the function

I like to keep track of the current frame up here → **CF: G**



There are 3 types of things you should be able to draw out

`bob = 3`

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

`def rob(bob):`
 `a = 2`
 `return 'mob'`

DEF STATEMENTS

1. Write the function name in the current frame
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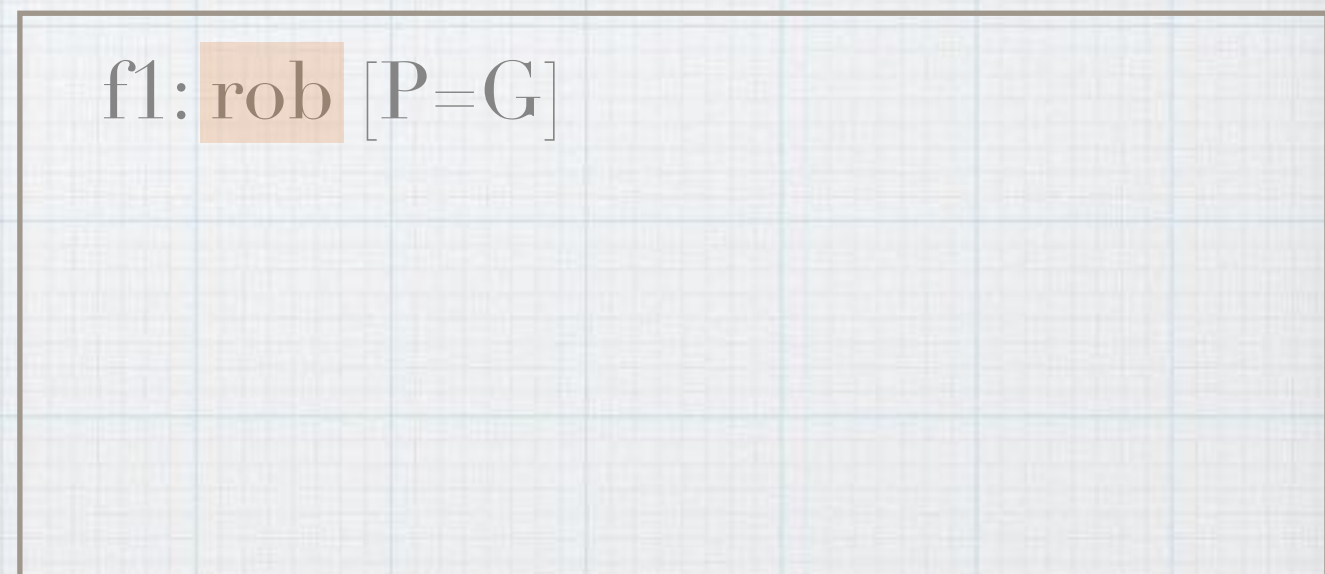
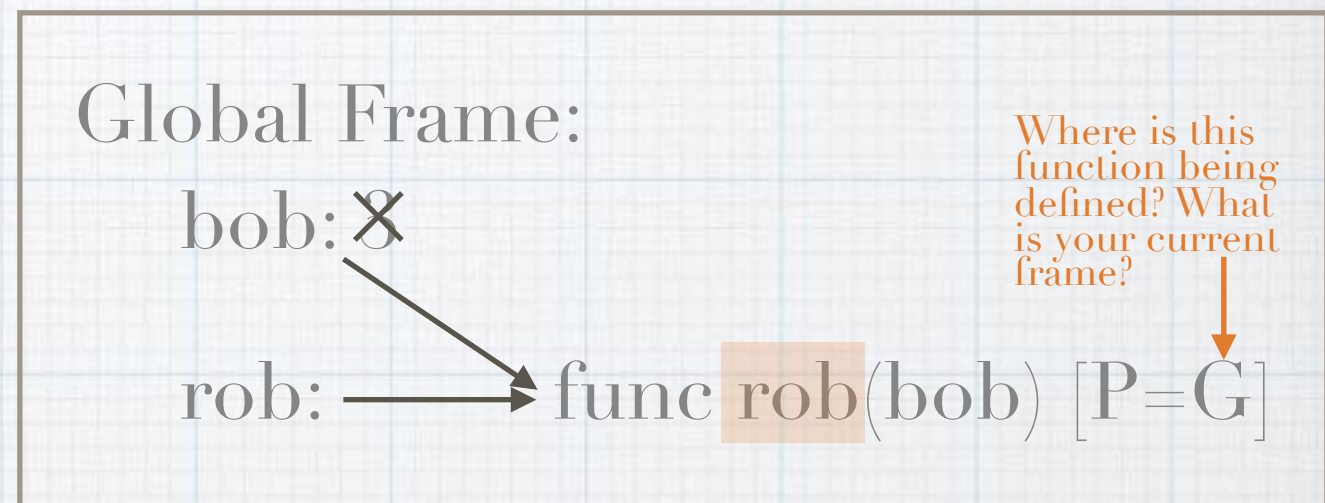
`bob = rob` What will this ASSIGNMENT do?

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(optional; update your current frame in CF:)
Assign the parameters
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I like to keep track of the current frame up here → CF: G, **f1**



There are 3 types of things you should be able to draw out

`bob = 3`

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

`def rob(bob):`
 `a = 2`
 `return 'mob'`

DEF STATEMENTS

1. Write the function name in the current frame
2. Point it to the function object which we represent by the function signature + parent

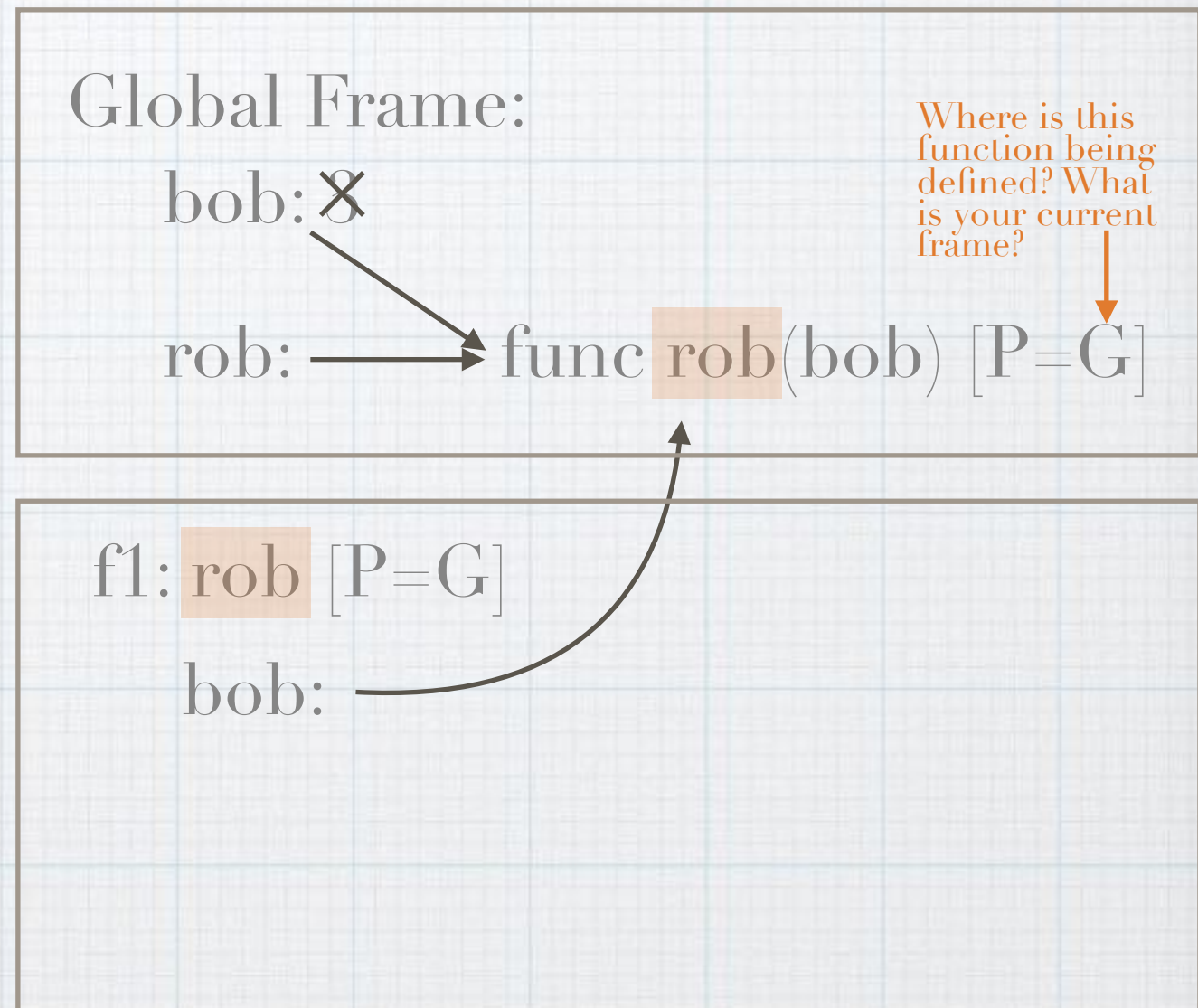
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Write f#: function name [P = ???]
(optional; update your current frame in CF:)
Assign the parameters
3. Execute the body of the function

I like to keep track of the current frame up here → CF: G, f1



There are 3 types of things you should be able to draw out

`bob = 3`

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

`def rob(bob):`
`a = 2`
`return 'mob'`

DEF STATEMENTS

1. Write the function name in the current frame
2. Point it to the function object which we represent by the function signature + parent

`bob = rob` What will this ASSIGNMENT do?

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1. Evaluate the operator and operand
2. Open a new frame
 Write f#: function name [P = ???]
 (optional; update your current frame in CF:)
Assign the parameters
3. Execute the body of the function

I like to keep track of the current frame up here → CF: G, ~~f~~ cross out a frame when you return

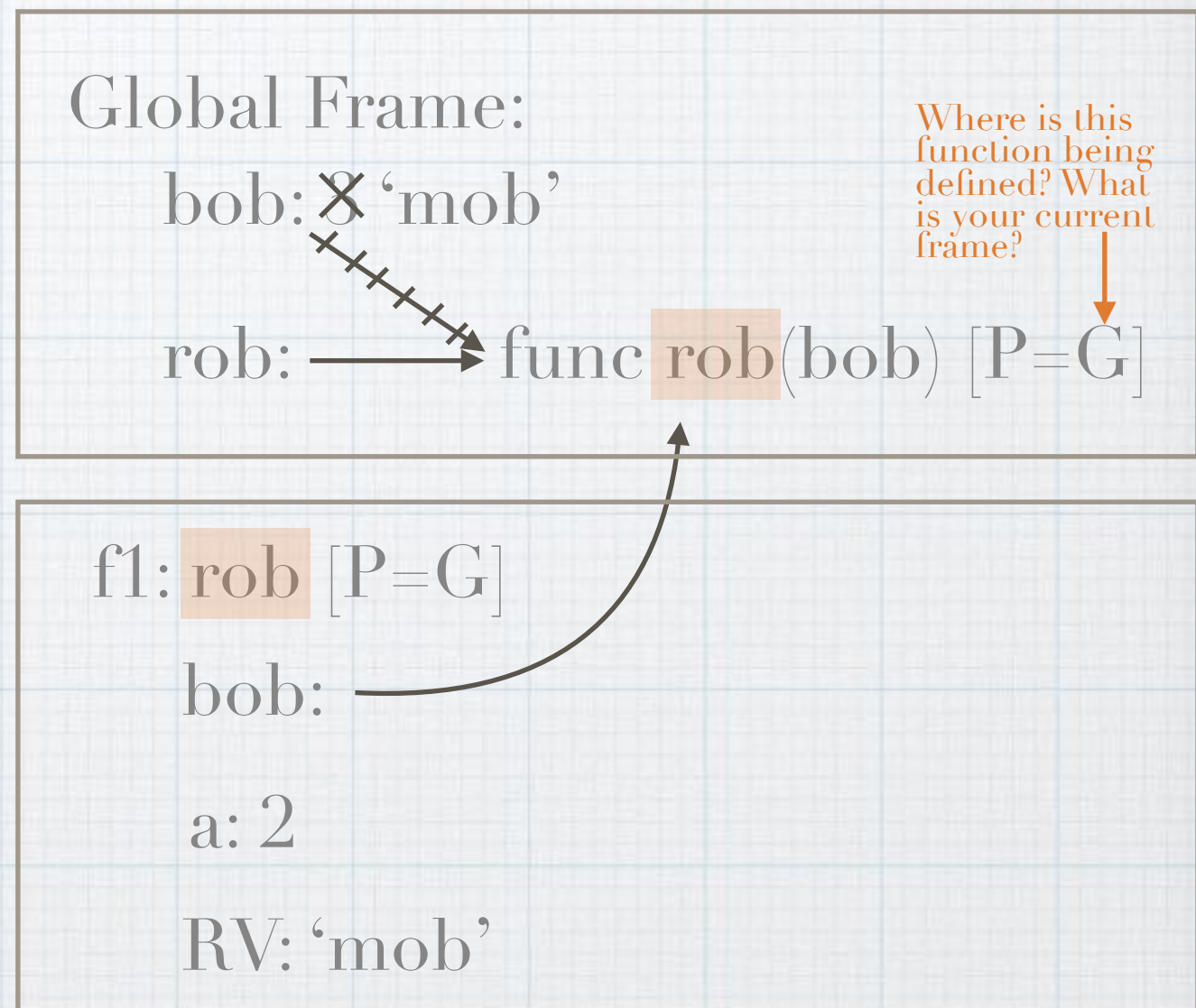


Diagram Rules

ASSIGNMENT

1. Evaluate the RHS
2. Write the name and value in the **current frame**

DEF STATEMENTS

1. Write the function name in the current frame
2. Point it to the function object which we represent by the function signature + parent

FUNCTION CALLS

1. Evaluate the operator and operand
2. Open a new frame

Write f#: function name
[P = ???]

(optional; update your current frame in CF:)

Assign the parameters

3. Execute the body of the function

3.1 #1

```
a = 1
def b(b):
    return a + b
a = b(a)
a = b(a)
```

tip: take it a line at a time

3.1 #1

Just executed
the first two
lines

→ a = 1

→ def b(b):
 return a + b

a = b(a) ← This is an
a = b(a) assignment. To
find the value
of the RHS we
need to do a
function call.

Before opening a new
frame, make sure you know
what the values of the
operator and operands are
(here a is 1 since that is its
value in the **global frame**)

CF: G

Global Frame:

a: 1

b → func b(b) [P=G]

tip: take it a line at a time

3.1 #1

```
→ a = 1
→ def b(b):
    return a + b
→ a = b(a)
   a = b(a)
```

To evaluate the body of the function, we need to do $a + b$. Since there is no a defined in $f1$ (the **current frame**) we must look for a in its parent

CF: G, f1

Global Frame:

a: 1

b → func b(**b**) [P=G]

f1: b [P=G]

b: 1

Note: The parameter is always just copied from the function signature up here. Even though we pass in a , we do not write a as the name of the parameter.

tip: take it a line at a time

3.1 #1

```
→ a = 1
→ def b(b):
    return a + b
→ a = b(a)
   a = b(a)
```

To evaluate the body of the function, we need to do $a + b$. Since there is no a defined in $f1$ (the **current frame**) we must look for a in its parent

CF: G, \emptyset

Global Frame:

a: 1

b → func b(b) [P=G]

f1: b [P=G]

b: 1

RV: 2 ($a + b = 1 + 1 = 2$)

tip: take it a line at a time

3.1 #1

Now we are finally ready to do the assignment. We know that `b(a)` evaluates to 2 (since this is the return value of `f1`) and we can reassign `a` to be 2 in the global frame

```
→ a = 1
→ def b(b):
    return a + b
→ a = b(a)
   a = b(a)
```

CF: G, ✕

Global Frame:

a: ✕, 2

b → func b(b) [P=G]

f1: b [P=G]

b: 1

RV: 2 ($a + b = 1 + 1 = 2$)

tip: take it a line at a time

3.1 #1

→ a = 1
→ def b(b):
 return a + b
→ a = b(a)
→ a = b(a) ← Another
 assignment and
 function call

CF: G, ✕

Global Frame:

a: ✕, 2

b → func b(b) [P=G]

f1: b [P=G]

b: 1

RV: 2

tip: take it a line at a time

3.1 #1

```
→ a = 1
→ def b(b):
    return a + b
→ a = b(a)
→ a = b(a)
```

CF: G, ~~A~~, ~~B~~

Global Frame:

a: ~~X~~, ~~X~~, 4

b → func b(b) [P=G]

f1: b [P=G]

b: 1

RV: 2

f2: b [P=G]

b: 2

RV: 4 (a + b = 2 + 2 = 4)

Notice that b is
2 here now,
since the global
a has changed

tip: take it a line at a time

3.1 #1

```
→ a = 1
→ def b(b):
    return a + b
→ a = b(a)
→ a = b(a)
```

Make sure that every frame has a return value!

CF: G, ~~A~~, ~~B~~

Global Frame:

a: ~~X~~, ~~X~~, 4

b → func b(b) [P=G]

f1: b [P=G]

b: 1

RV: 2

f2: b [P=G]

b: 2

RV: 4

tip: take it a line at a time

3.1 #2

```
def curry2(h):  
    def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    return f  
  
make_adder = curry2(add)  
  
add_three = make_adder(3)  
  
five = add_three(2)
```

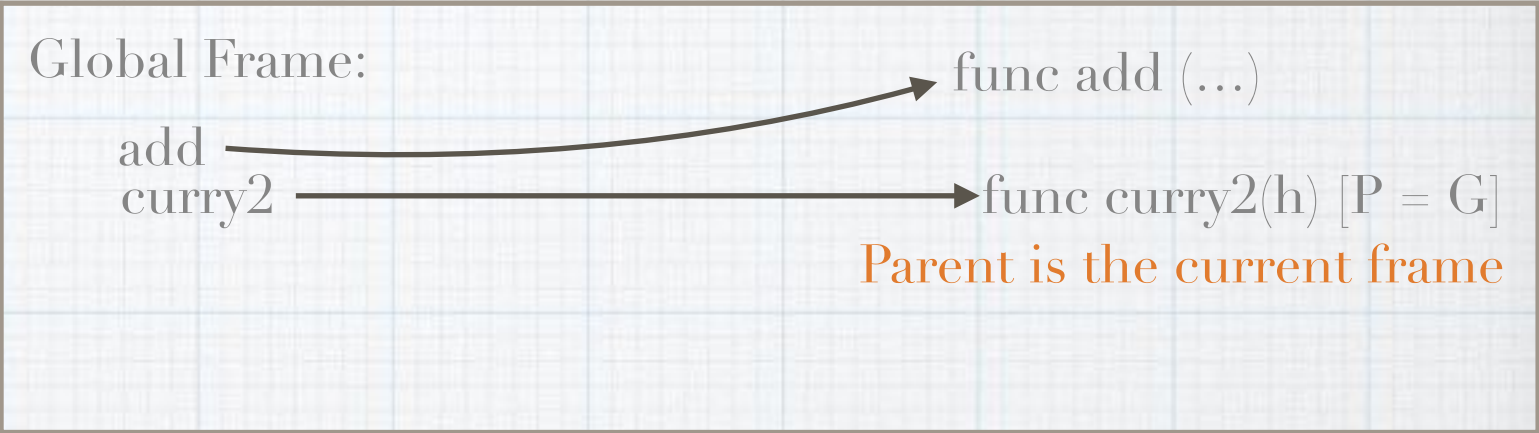
tip: when you start doing a function call, remember where you were before

3.1 #2

CF: G

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    return f  
  
make_adder = curry2(add)  
add_three = make_adder(3)  
five = add_three(2)
```



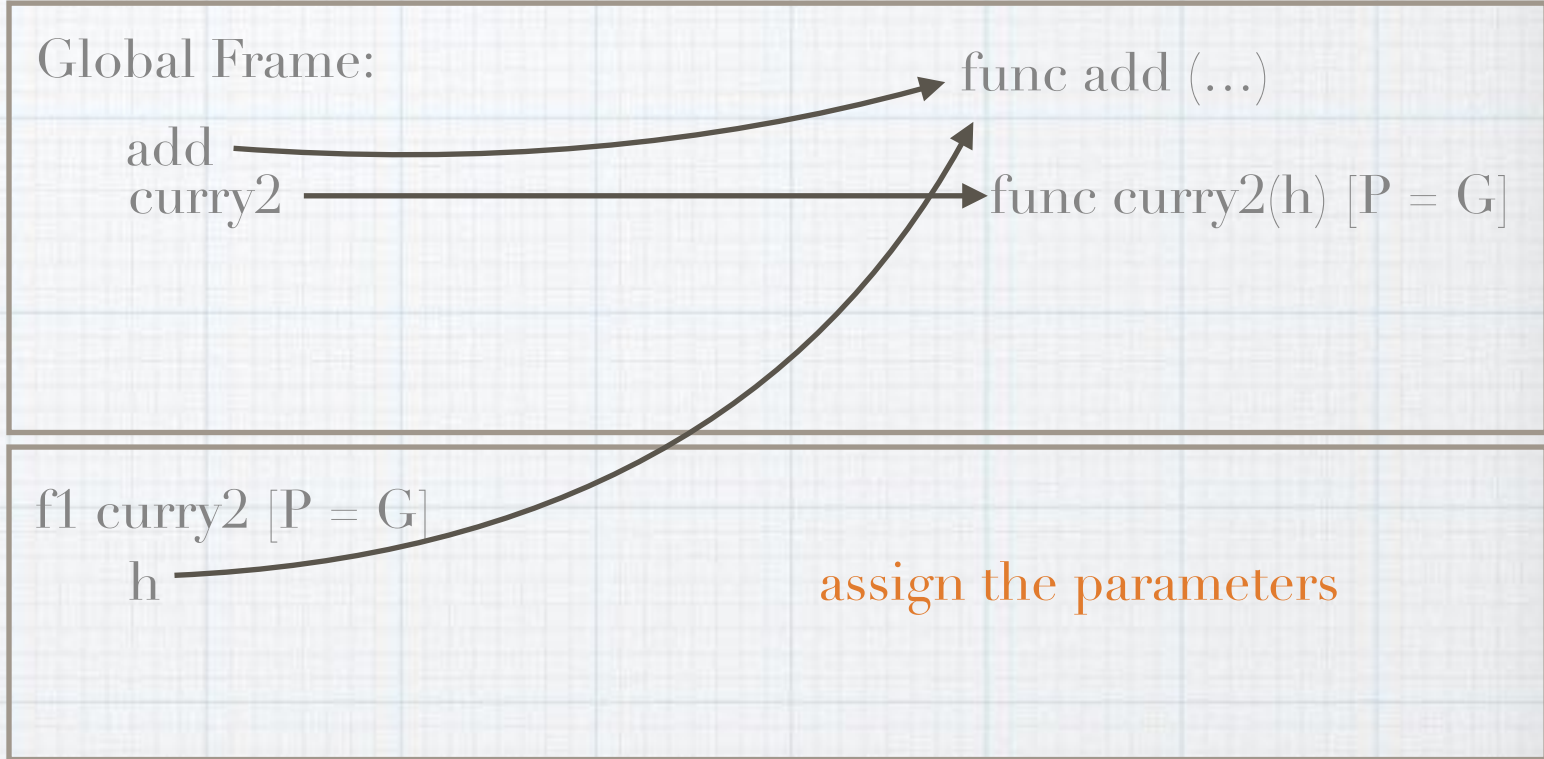
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3.1 #2

CF: G, f1

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    return f  
  
→ make_adder = curry2(add)  
add_three = make_adder(3)  
five = add_three(2)
```



- Recall function calls:
1. Evaluate operator and operands,
 2. Create a new frame
 3. Assign the parameters in the new frame

tip: when you start doing a function call, remember where you were before

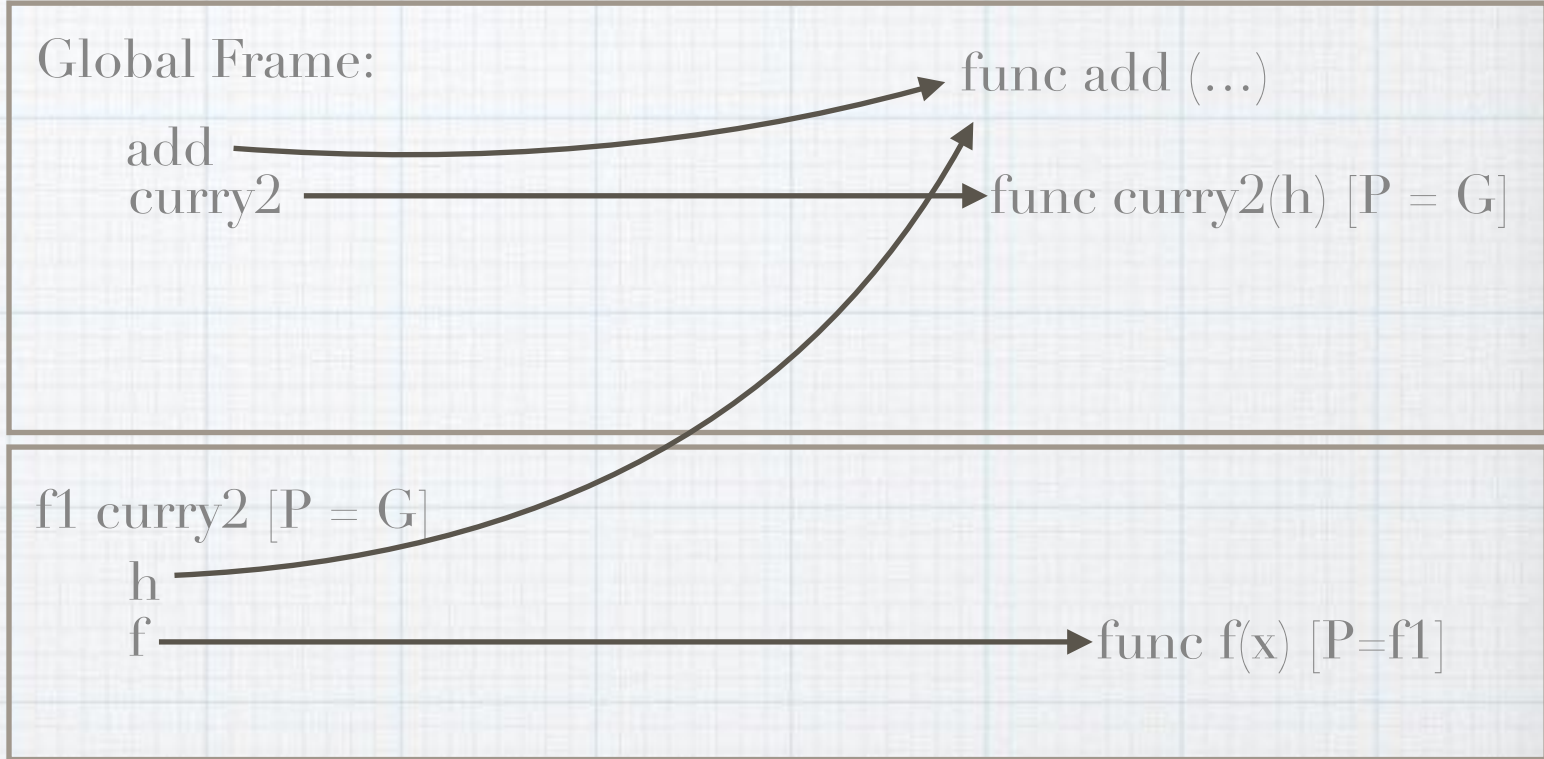
3.1 #2

CF: G, f1

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
def curry2(h):  
    def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    return f
```

Inside curry2 we define a new function, f. What is its parent?



```
make_adder = curry2(add)  
add_three = make_adder(3)  
five = add_three(2)
```

- Recall function calls:
1. Evaluate operator and operands,
 2. Create a new frame
 3. Assign the parameters in the new frame

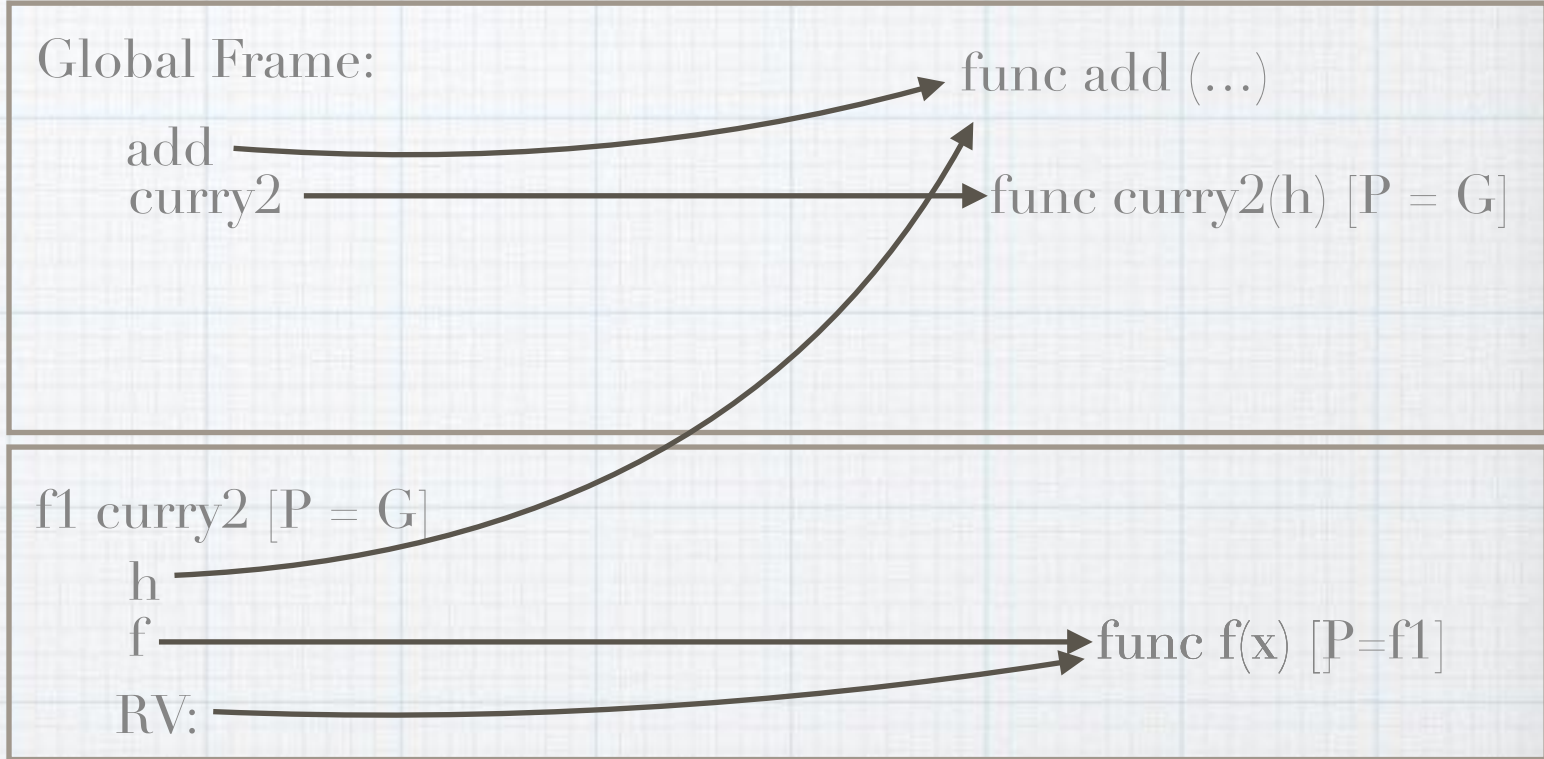
tip: when you start doing a function call, remember where you were before

3.1 #2

CF: G, ~~∅~~

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    → return f  
→ make_adder = curry2(add)  
add_three = make_adder(3)  
five = add_three(2)
```



now we return the function we just defined

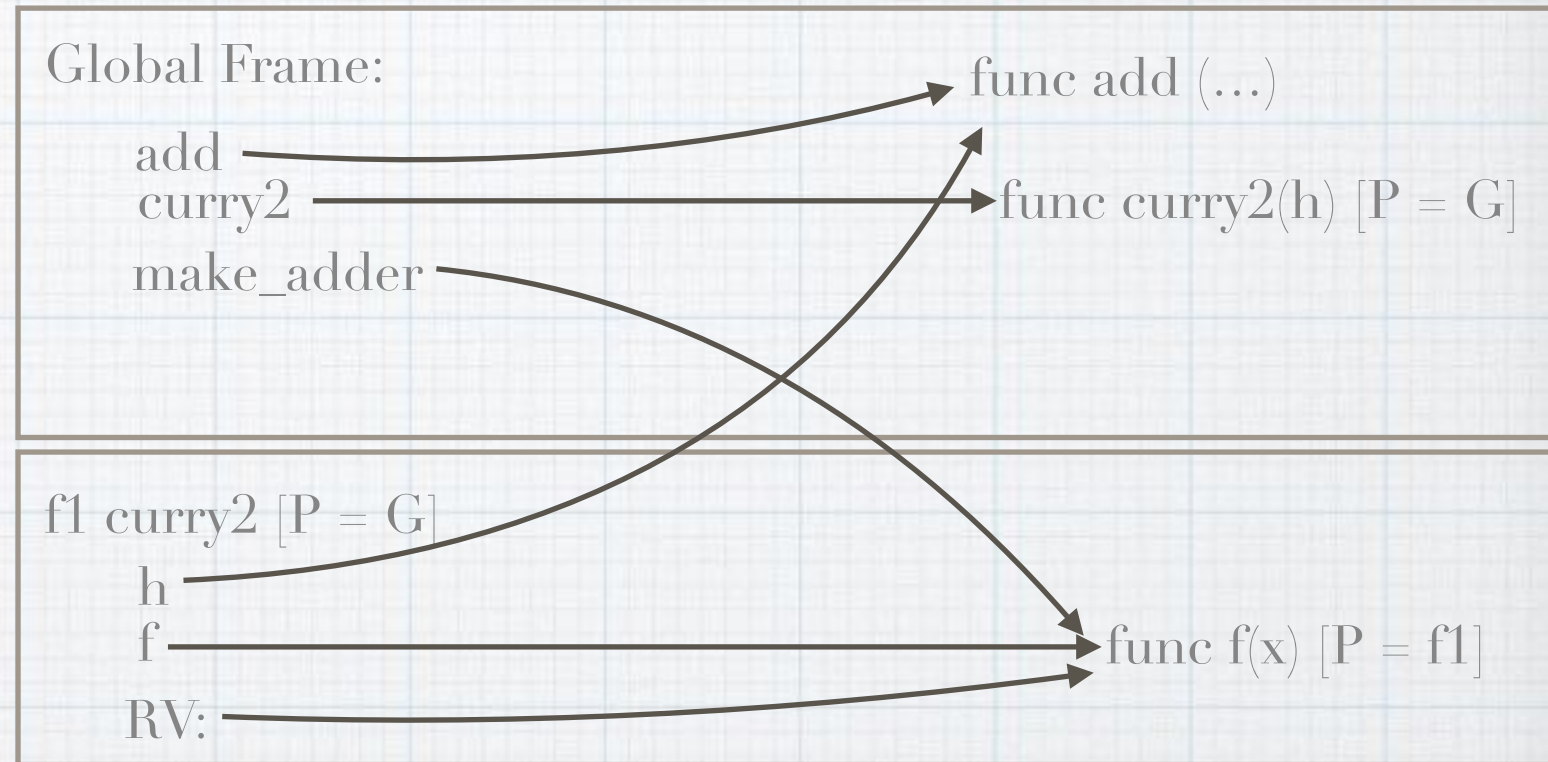
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3.1 #2

CF: G, ⌘

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    → return f  
→ make_adder = curry2(add)  
add_three = make_adder(3)  
five = add_three(2)
```



finally assign the value that `curry2` returned to `make_adder`

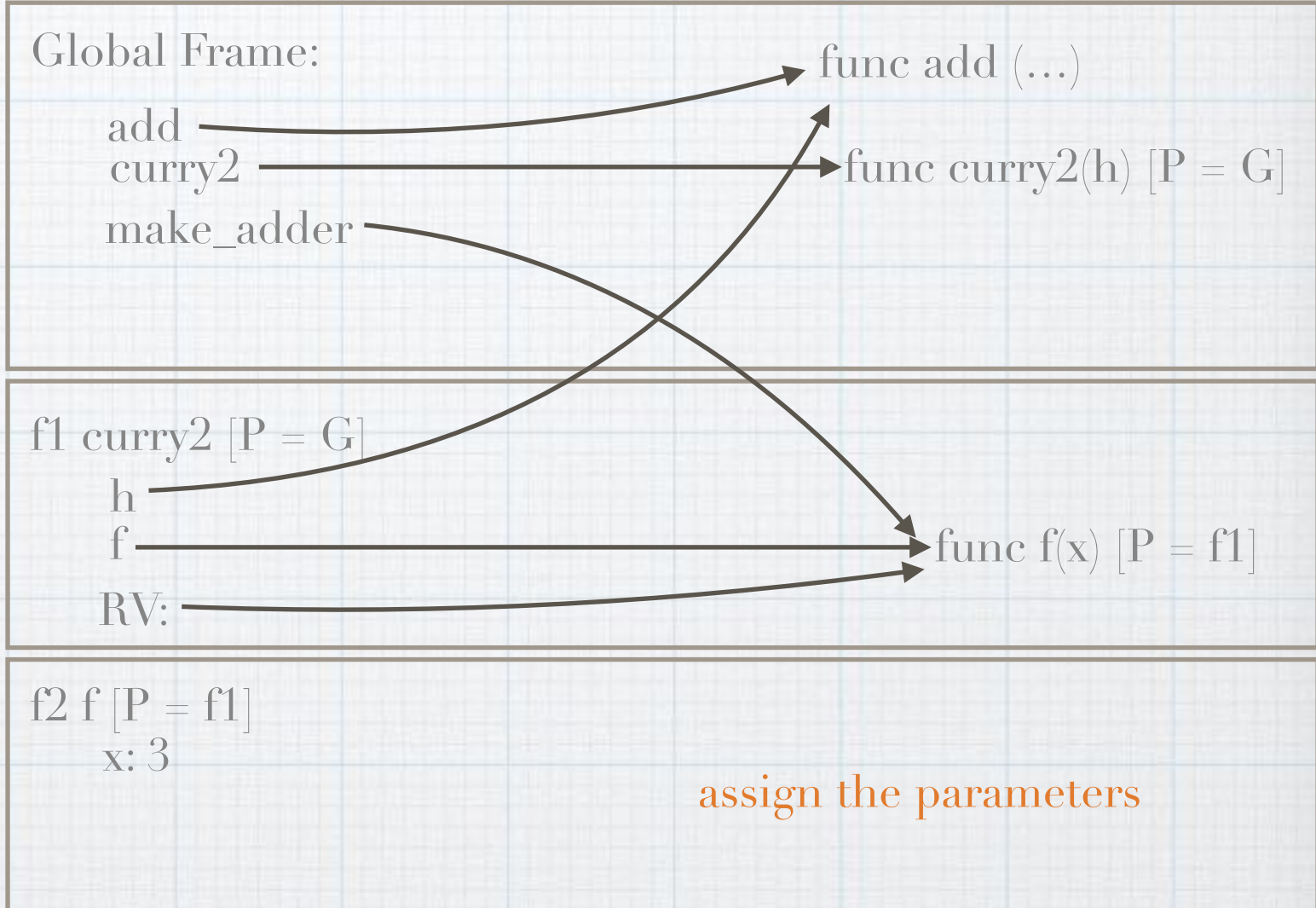
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3.1 #2

CF: G, f1, f2

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    → return f  
→ make_adder = curry2(add)  
→ add_three = make_adder(3)  
five = add_three(2)
```



tip: when you start doing a function call, remember where you were before

3.1 #2

CF: G, f1, f2

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

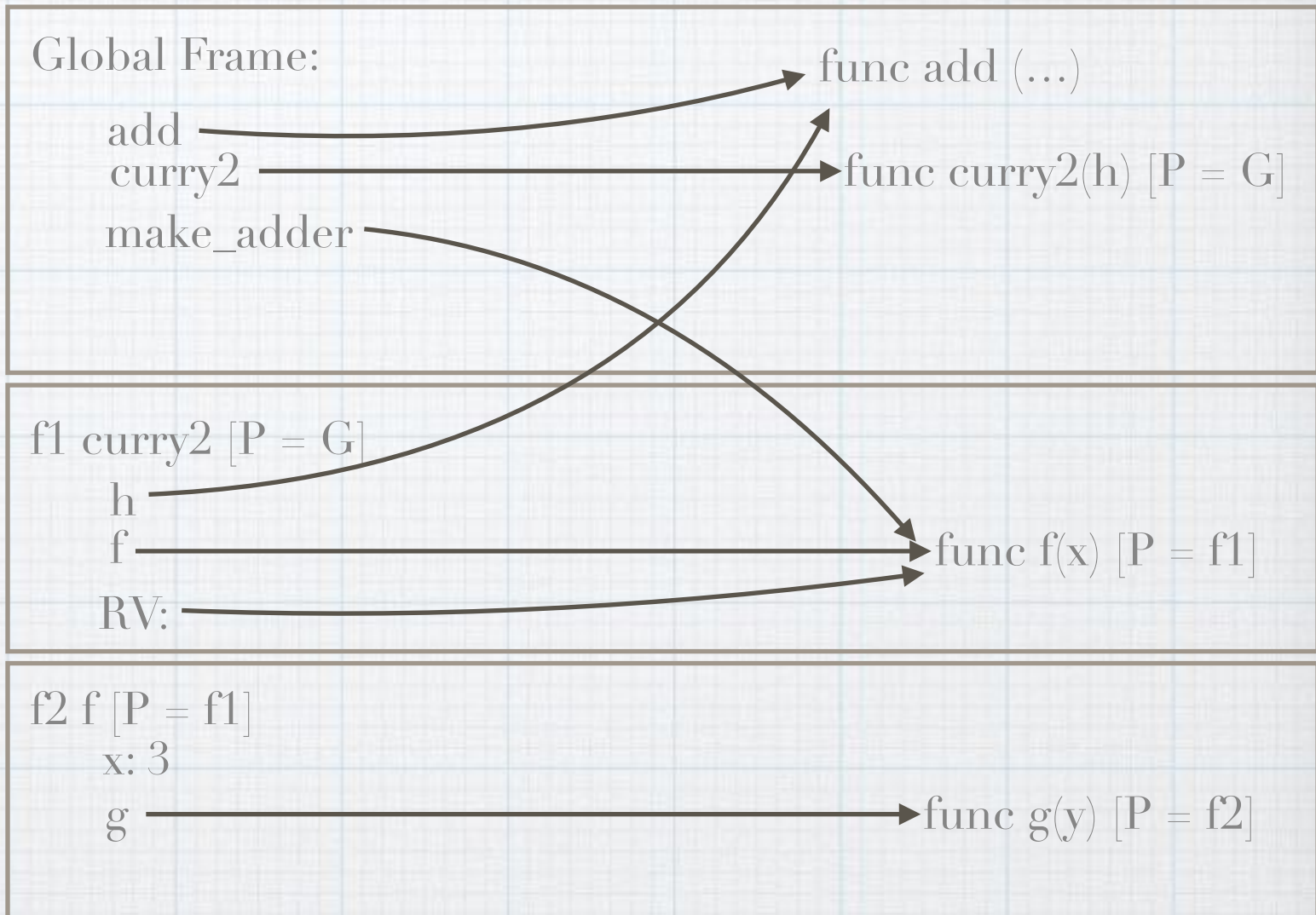
```
def curry2(h):  
    def f(x):  
        def g(y):  
            return h(x, y)  
        return g  
    return f
```

Inside f we define a new function, g. What is its parent?

```
make_adder = curry2(add)
```

```
add_three = make_adder(3)
```

```
five = add_three(2)
```



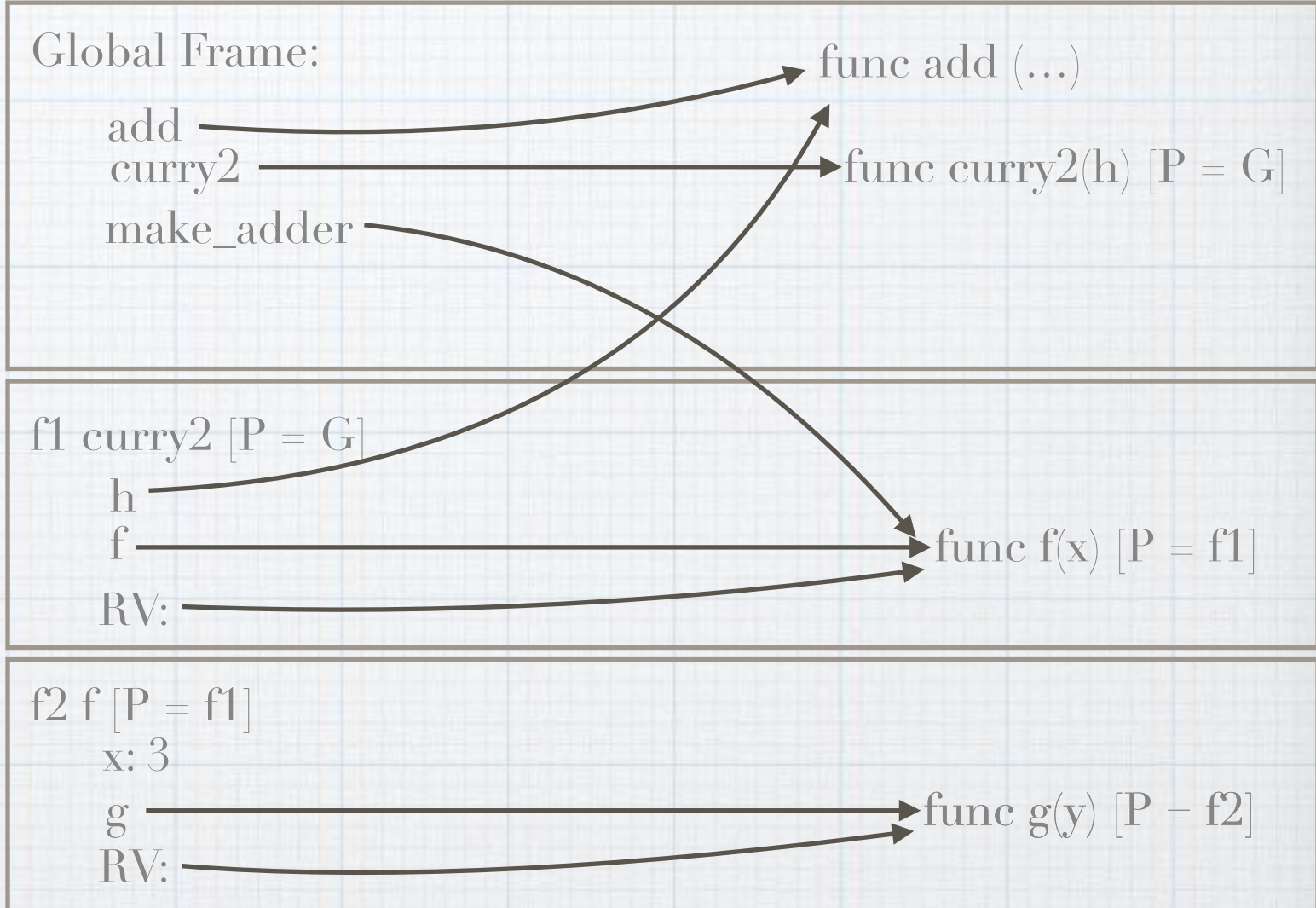
tip: when you start doing a function call, remember where you were before

3.1 #2

CF: G, ~~G~~, ~~G~~

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        → def g(y):  
            return h(x, y)  
        → return g  
    → return f  
→ make_adder = curry2(add)  
→ add_three = make_adder(3)  
five = add_three(2)
```



now we return the function we just defined

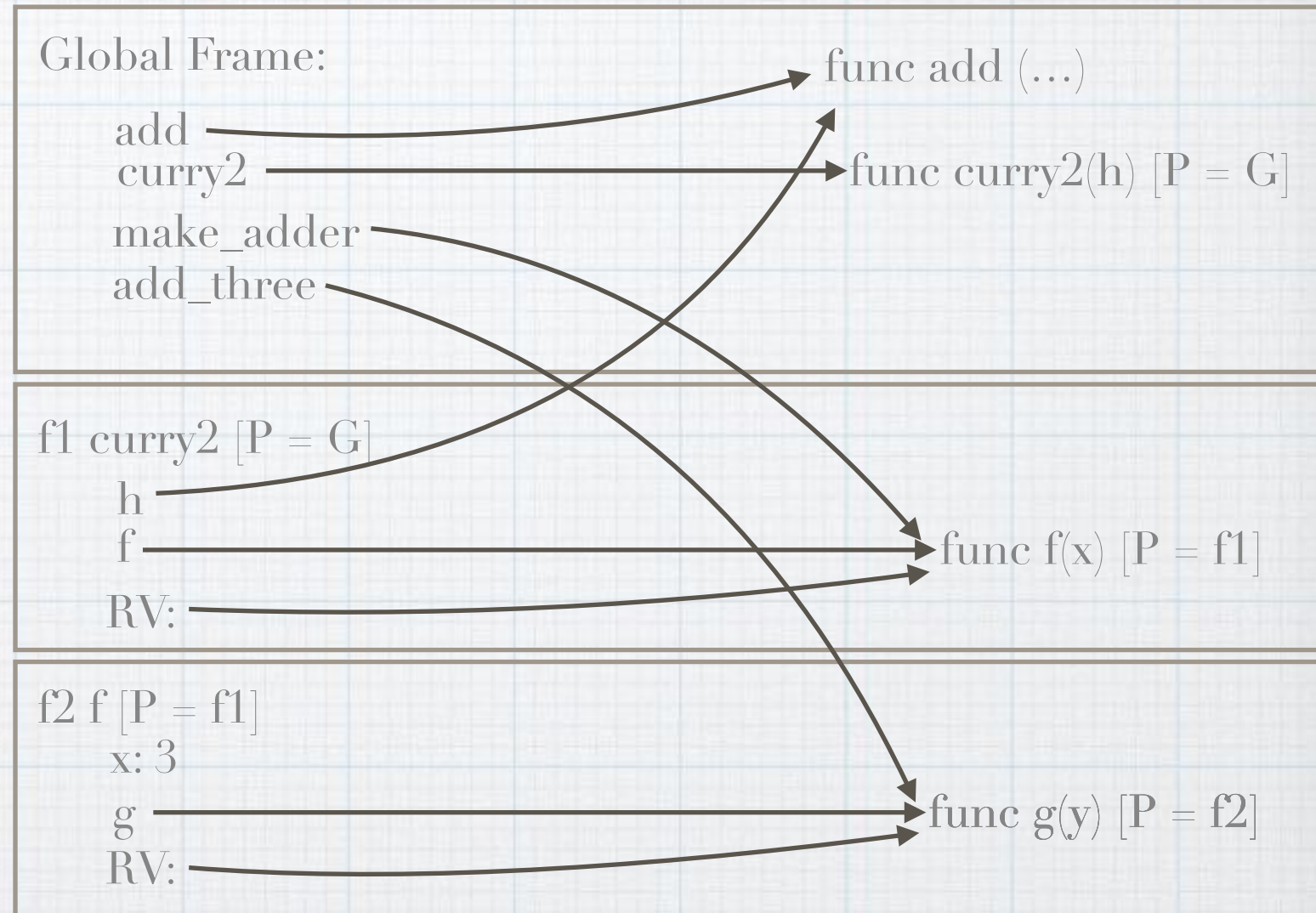
tip: when you start doing a function call, remember where you were before

3.1 #2

CF: G, ~~G~~, ~~G~~

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        → def g(y):  
            return h(x, y)  
        → return g  
    → return f  
→ make_adder = curry2(add)  
→ add_three = make_adder(3)  
five = add_three(2)
```



finally, assign the return value to `add_three`

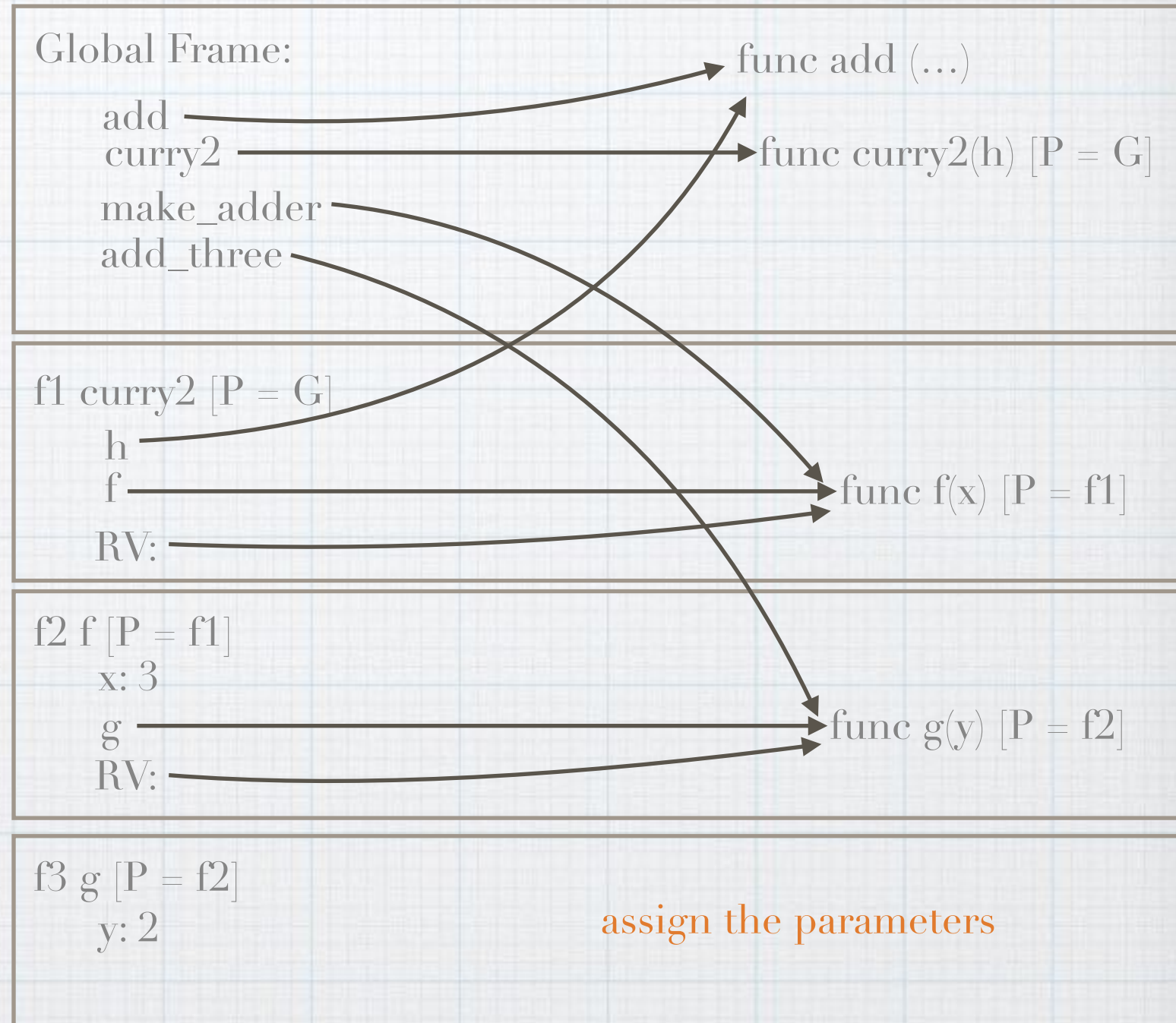
tip: when you start doing a function call, remember where you were before

3.1 #2

CF: G, ~~⊗~~

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        → def g(y):  
            → return h(x, y)  
        → return g  
    → return f  
→ make_adder = curry2(add)  
→ add_three = make_adder(3)  
→ five = add_three(2)
```



tip: when you start doing a function call, remember where you were before

3.1 #2

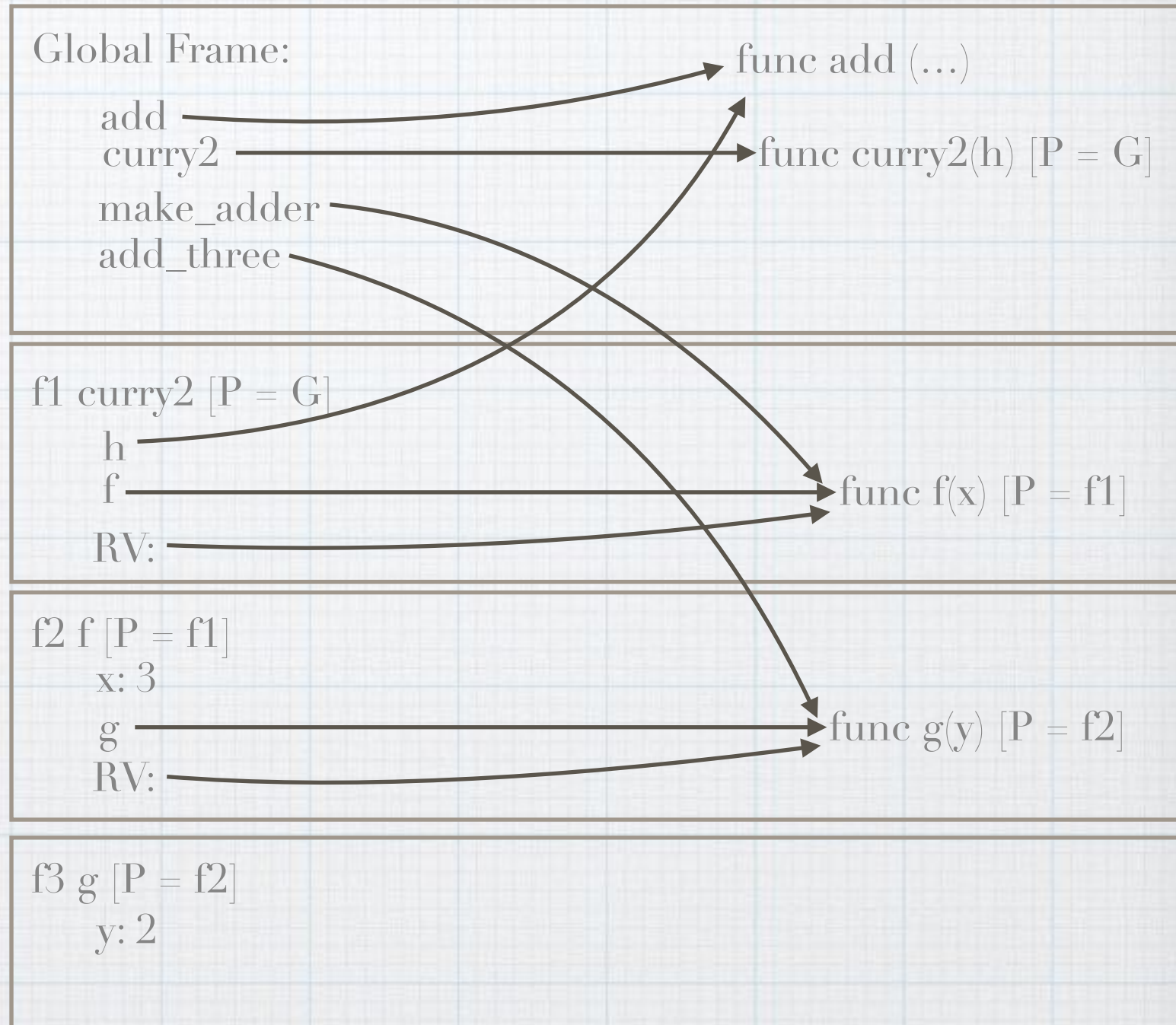
CF: G, ~~⊗~~

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        → def g(y):  
            → return h(x, y)  
        → return g  
    → return f  
→ make_adder = curry2(add)  
→ add_three = make_adder(3)  
→ five = add_three(2)
```

Here we call $h(x, y)$ but we do not draw a new frame for it. Why?

What are x and y ?



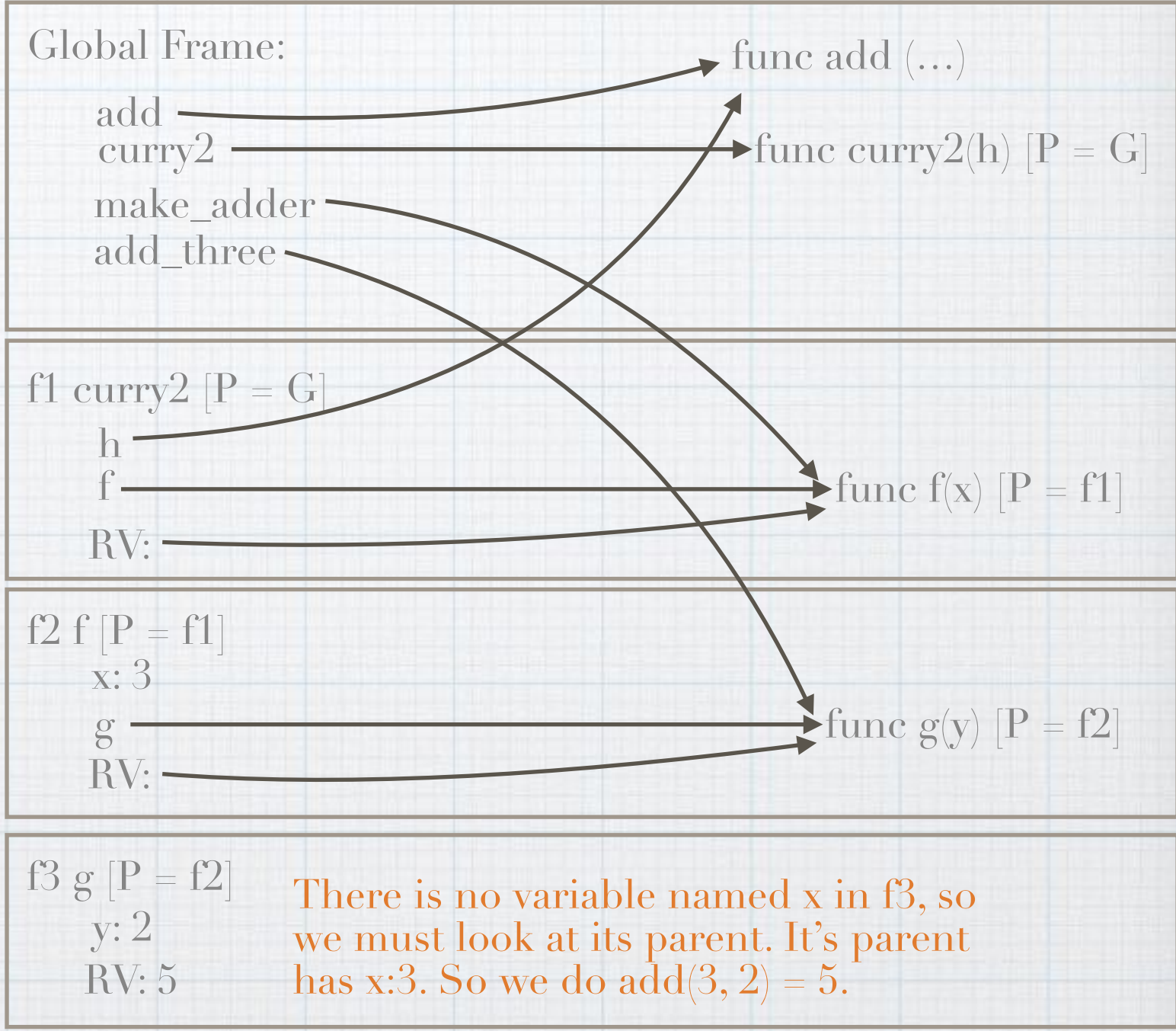
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3.1 #2

CF: G, ~~⊗~~

I like to draw a line here so that I don't accidentally start evaluating the body of the def right away

```
→ def curry2(h):  
    → def f(x):  
        def g(y):  
            → return h(x, y)  
        return g  
    return f  
  
→ make_adder = curry2(add)  
→ add_three = make_adder(3)  
→ five = add_three(2)
```



tip: when you start doing a function call, remember where you were before

3.1 #2

CF: G, ~~⌘~~

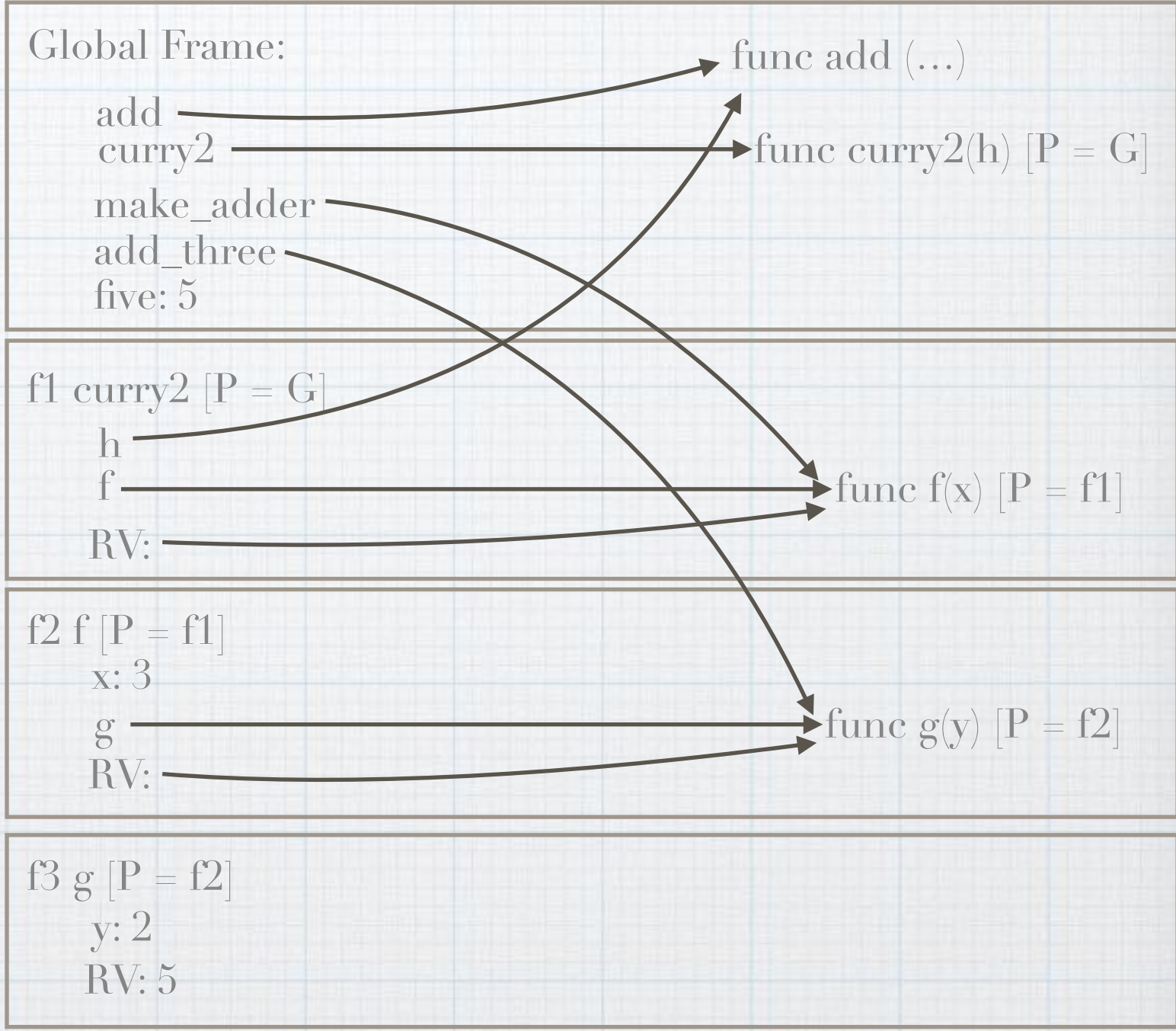
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```
→ def curry2(h):  
    → def f(x):  
        def g(y):  
            → return h(x, y)  
        return g  
    return f  
→ make_adder = curry2(add)  
→ add_three = make_adder(3)  
→ five = add_three(2)
```

return the result of add(3, 2)

function call

assignment



tip: when you start doing a function call, mark where you were before so that you know which line to go back to